# **CSI5180.** Machine Learning for Bioinformatics Applications

**Ensemble** Learning

Marcel Turcotte

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# Preamble

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#### **Ensemble Learning**

In this lecture, we consider several meta learning algorithms all based on the principle that the combined opinion of a large group of individuals is often more accurate than the opinion of a single expert — this is often referred to as the **wisdom of the crowd**. Today, we tell apart the following meta-algorithms: **bagging**, **pasting**, **random patches**, **random subspaces**, **boosting**, and **stacking**.

#### General objective :

**Compare** the specific features of various ensemble learning meta-algorithms

### Learning objectives

- Discuss the intuition behind bagging and pasting methods
- **Explain** the difference between random patches and random subspaces
- **Describe** boosting methods
- **Contrast** the stacking meta-algorithms from bagging

#### Reading:

Jaswinder Singh, Jack Hanson, Kuldip Paliwal, and Yaoqi Zhou. RNA secondary structure prediction using an ensemble of two-dimensional deep neural networks and transfer learning. *Nature Communications* **10**(1):5407, 2019.

### www.mims.ai



#### Bioinformatician/ Bioinformatics analyst

Institution/Compa	My Intelligent Machines (MIMs)	
Location:	Montreal, QC, Canada	
Job Type:	Programmer/Developer	
Degree Level Requ	Masters, Bachelor's, PhD	Apply No

#### **Bioinformatician/ Bioinformatics analyst**

My Intelligent Machines (MIMs) is looking for a highly talented senior bioinformatician/bioinformatics analysts to participate at the development of the core of a world class platform for life scientist integrating AI, Natural language, domain specific workflows. In this role, you will work closely with the AI and Bioinfo teams to provide the state-of-art technology to life scientists. This full time position will focus on workflow design, data/results integration and graphical representation.

**Responsibilities:** 

#### bioinformatics.ca/job-postings



#### 1. Preamble

#### 2. Introduction

#### 3. Justification

#### 4. Meta-algorithms

#### 5. Prologue

# Introduction

\* "Ensemble learning is a learning paradigm that, instead of trying to learn one super-accurate model, focuses on training a large number of low-accuracy models and then combining the predictions given by those weak models to obtain a high-accuracy meta-model." [Burkov, 2019] §7.5

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- Weak learners (low-accuracy) models are simple and fast, both for training and prediction.
- The general idea is that each learner has a vote, and these votes are combined to establish the final decision.
- **Decision trees** are the most commonly used weak learners.
- Ensemble learning is fact an umbrella for a large family of meta-algorithms, including bagging, pasting, random patches, random subspaces, boosting, and stacking.

# **Justification**

10 experiments

#### 10 experiments

Each experiment consists of tossing a loaded coin

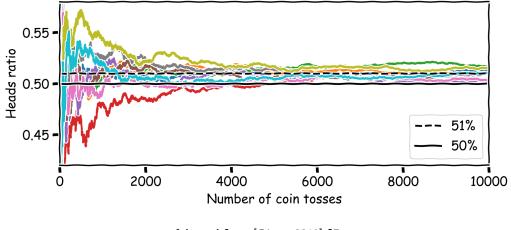
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  - 51 % head, 49 % tail
- $\blacktriangleright$  As the number of toss increases, the proportion of heads will approach 51%

```
tosses = (np.random.rand(10000, 10) < 0.51). astype(np.int8)
cumsum = np.cumsum(tosses, axis=0) / np.arange(1, 10001).reshape(-1, 1)
with plt.xkcd():
    plt.figure(figsize = (8, 3.5))
    plt.plot(cumsum)
    plt.plot([0, 10000], [0.51, 0.51], "k-", linewidth=2, label="51%")
    plt.plot([0, 10000], [0.5, 0.5], "k-", label="50%")
    plt.xlabel("Number of coin tosses")
    plt.ylabel("Heads ratio")
    plt.legend(loc="lower right")
    plt.axis([0, 10000, 0.42, 0.58])
    plt.tight_layout()
    plt.savefig("weak learner.pdf", format="pdf", dpi=264)
```



Adapted from [Géron, 2019] §7

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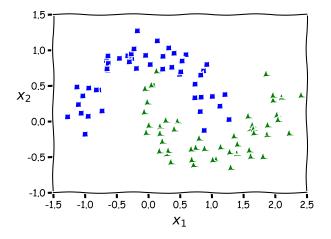
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  - Different algorithms
  - Different sets of features
  - Different data sets

### Data set - moons

```
import matplotlib.pyplot as plt
from sklearn datasets import make_moons
X, y = make moons(n samples=100, noise=0.15)
with plt.xkcd():
    plt.plot(X[:, 0][y==0], X[:, 1][y==0], "bs")
    plt.plot(X[:, 0][y==1], X[:, 1][y==1], "g^")
    plt.axis([-1.5, 2.5, -1, 1.5])
    plt.grid(True, which='both')
    plt.xlabel(r"$x 1$", fontsize=20)
    plt.ylabel(r"$x 2$", fontsize=20, rotation=0)
    plt.tight layout()
    plt.savefig("make moons.pdf", format="pdf", dpi=264)
```

Adapted from: [Géron, 2019] §5

### Data set - moons

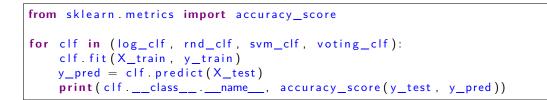


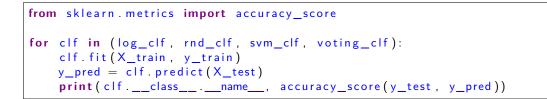
Adapted from [Géron, 2019] §5

### Source code - VotingClassifier - hard

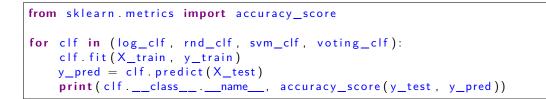
```
from sklearn ensemble import VotingClassifier
from sklearn.ensemble import RandomForestClassifier
from sklearn linear_model import LogisticRegression
from sklearn.svm import SVC
\log_clf = LogisticRegression()
rnd clf = RandomForestClassifier()
svm_clf = SVC()
estimators = [('lr', log clf),
            ('rf', rnd_clf),
('svc', svm_clf)]
voting_clf = VotingClassifier (estimators=estimators, voting='hard')
voting clf.fit(X_train, y_train)
```

#### Source: [Géron, 2019] §7





```
LogisticRegression 0.864
RandomForestClassifier 0.896
SVC 0.888
VotingClassifier 0.904
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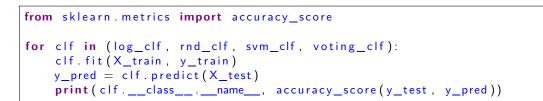
[Géron, 2019] §7

### Source code - VotingClassifier - soft

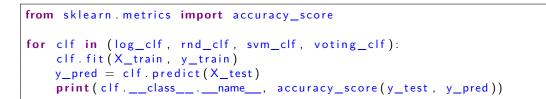
```
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from sklearn.ensemble import RandomForestClassifier
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\log_clf = LogisticRegression()
rnd clf = RandomForestClassifier()
svm clf = SVC(probability=True)
estimators = [('lr', log clf),
            ('rf', rnd_clf),
('svc', svm_clf)]
voting_clf = VotingClassifier(estimators=estimators, voting='soft')
voting clf.fit(X_train, y_train)
```

#### Source: [Géron, 2019] §7

### **Source code - accuracy**

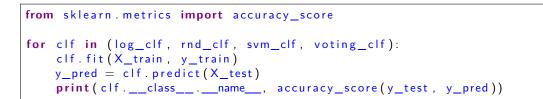


### **Source code - accuracy**



```
LogisticRegression 0.864
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VotingClassifier 0.92
```

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```

Soft uses the average probability score, rather than hard voting. [Géron, 2019] §7

# **Meta-algorithms**

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- As an added bonus, the learns can be trained in **parallel**!
- Literature suggests that **bagging** outperforms **pasting** [Géron, 2019].

## sklearn.ensemble.BaggingClassifier

- **Soft voting** by default
- bootstrap=False implies pasting

Adapted from: [Géron, 2019] §7

- Bagging and pasting apply for regression tasks as well.
  - **BaggingRegressor** in Keras
  - Voting is replaced the average





#### Claim:

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- By default, bagging samples N examples with replacement, where N is the size of the training set.

```
from random import random
def do_sample_with_replacement():
    xs = [1 \text{ for } i \text{ in } range(100)]
    for sample in range(100):
        index = int(100 * random())
        xs[index] = 0
    print(sum(xs))
for run in range (10):
    do sample with replacement()
```

## **Empirical evidence**

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0.9013333333333333322

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  - **Random patches:** sampling **both** instances and features.

```
bag_clf = BaggingClassifier(
    DecisionTreeClassifier(), n_estimators=500,
    bootstrap=True, max_samples=1.0,
    bootstrap_features=True, max_features=0.4,
    n_jobs=-1, oob_score=True)
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        n_jobs=-1, oob_score=True)
```

**Random subspaces: only** sampling features.

```
bag_clf = BaggingClassifier(
    DecisionTreeClassifier(splitter="random", max_leaf_nodes=16),
    n_estimators=500, max_samples=1.0, bootstrap=True)
```

### sklearn.ensemble.RandomForestClassifier

"The Random Forest algorithm introduces extra randomness when growing trees; instead of searching for the very best feature when splitting a node (...), it searches for the best feature among a random subset of features." [Géron, 2019]

```
from sklearn.ensemble import RandomForestClassifier
rfc = RandomForestClassifier(n_estimators=500, max_leaf_nodes=16)
rfc.fit(X_train, y_train)
y_pred_rf = rfc.predict(X_test)
```

#### See also ExtraTreesClassifier and ExtraTreesRegressor.

Boosting meta-algorithms are training learners sequentially, in such a way that each classifier is trying to correct the mistakes of the previous classifier in the chain.

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  - Specifically, the weight of examples incorrectly is increased with each iteration.
  - Initially, the weight of each example  $(w_i)$  is  $\frac{1}{N}$ , where N is the number of examples.

### AdaBoost - error rate

Let's define an **indicator function**:

$$I(\hat{y}_{i}^{(j)}, y_{i}) = \begin{cases} 0 & \text{if } \hat{y}_{i}^{(j)} = y_{i} \\ 1 & \text{if } \hat{y}_{i}^{(j)} \neq y_{i} \end{cases}$$

where  $\hat{y}_i^{(j)}$  is the prediction of the  $j^{\text{th}}$  learner on example *i* and  $y_i$  is the label of example *i*.

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where  $\hat{y}_i^{(j)}$  is the prediction of the  $j^{\text{th}}$  learner on example *i* and  $y_i$  is the label of example *i*.

The **error rate** of the *j*<sup>th</sup> learner is defined as:

$$r_{j} = \frac{\sum_{i=1}^{N} w_{i} \times I(\hat{y}_{i}^{(j)}, y_{i})}{\sum_{i=1}^{N} w_{i}}$$

### AdaBoost - learner's weight

When making a final decision (vote), each learner has a weigth.

The **weight** of the learner *j*:

$$\alpha_j = \eta \log \frac{1 - r_j}{r_j}$$

where  $\eta$  is the learning rate, default value is 1.

- Low error rate implies high learn's weight.
- Random guesses, error rate = 0.5, implies a weight of 0.
- Error rate > 0.5 implies a negative weight.

After training the learner *j*, the weight of each example is updated as follows.

$$w_i = \begin{cases} w_i & \text{if } \hat{y}_i^{(j)} = y_i \\ w_i \times e^{\alpha_j} & \text{if } \hat{y}_i^{(j)} \neq y_i \end{cases}$$

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eq y_i \end{cases}$$

The weights are then normalized, dividing them by  $\sum_{i=1}^{N} w_i$ 

The outcome is the class with the **largest weighted vote**:

$$\hat{y}(x) = \operatorname{argmax}_k \sum_{\substack{j=1 \ \hat{y}^{(j)}(x)=k}}^m lpha_j$$

where m is the number of learners.

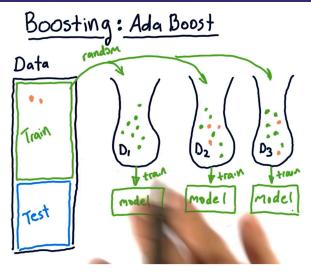
## sklearn.ensemble.AdaBoostClassifier

[Géron, 2019] §7

## AdaBoost

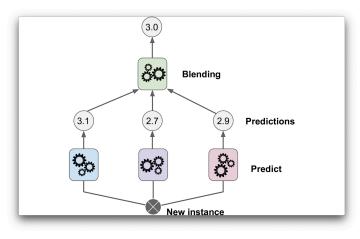
- A literature search using Scopus for "AdaBoost" and "bioinformatics returns 78 references. Including the following two papers:
  - Y. Qu, B.-L. Adam, Y. Yasui, M.D. Ward, L.H. Cazares, P.F. Schellhammer, Z. Feng, O.J. Semmes, and G.L. Wright Jr., Boosted decision tree analysis of surface-enhanced laser desorption/ionization mass spectral serum profiles discriminates prostate cancer from noncancer patients, *Clinical Chemistry* 48 (2002), no. 10, 18351843, cited By 382.
  - P.M. Long and V.B. Vega, Boosting and microarray data, *Machine Learning* 52 (2003), no. 1-2, 3144, cited By 40.

### AdaBoost



https://youtu.be/GM3CDQfQ4sw

# Stacking



Source [Géron, 2019] Figure 7.12

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- Unlike bagging, stacking does not use a predetermined function to combine the predictions, say majority vote, instead, it trains a classifier/regressor.
- A holdout set is used to train the blender.





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- **Boosting** combines the learners in a sequential, rather than parallel, manner. Each learner fixes the mistakes of its predecessor.



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- This diversity of learners can be achieved in various ways: different algorithms, different sets of features, (slightly) different data sets.
- **Boosting** combines the learners in a sequential, rather than parallel, manner. Each learner fixes the mistakes of its predecessor.
- With stacking, a learning algorithm is used to combine the results the weak classifiers.

#### Null

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Singh, J., Hanson, J., Heneman, R., Paliwai, K., Yang, Y., and Zhou, Y. (2016b). Detecting proline and non-proline cis isomers in protein structures from sequences using deep residual ensemble learning.

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Zhang, L., Yu, G., Xia, D., and Wang, J. (2019).

Protein-protein interactions prediction based on ensemble deep neural networks. *Neurocomputing*, 324:10–19.

Zhang, X., Wang, J., Li, J., Chen, W., and Liu, C. (2018). CrIncrc: a machine learning-based method for cancer-related long noncoding rna identification using integrated features. BMC Med Genomics, 11(Suppl 6):120. Zheng, R., Li, M., Chen, X., Wu, F.-X., Pan, Y., and Wang, J. (2019). BiXGBoost: a scalable, flexible boosting-based method for reconstructing gene regulatory networks. *Bioinformatics*, 35(11):1893–1900.



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